

# The pmdraw package\*

Matthias Fresacher  
matthias.ypg37@slmail.me

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## Abstract

The `pmdraw` package allows you to draw elements of the Partition Monoids, commonly referred to diagrams. The package provides a lot of flexibility to draw most diagrams and can be customised as needed.

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\*This document corresponds to `pmdraw` v1.0, 2023-11-08.

# 1 Introduction

## 1.1 Motivation

Partition monoids and their closely related algebras are well studied objects with applications in theoretical physics and representation theory in mathematics. The elements of these monoids are called diagrams because they can be drawn graphically as a graph following certain conventions.

My PhD thesis examines properties of these partition monoids and hence I needed to draw a large number of diagrams in a neat and consistent way. This thesis work formed the basis of this package with only customisability and the manual needed to be added to complete this package.

## 1.2 Acknowledgments

Most importantly, I thank James East, my PhD supervisor for allowing me to get a little sidetracked in my PhD research and develop and publish this package rather than work on my thesis like I should have.

This package has at its core the basic drawing macro of a diagram as used by James East and Nik Ruškuc in their 2022 publication *Classification of congruences of twisted partition monoids* in Advances in Mathematics. I thank them both for allowing me to build on their work.

I thank everybody that has helped me proof read, spot bugs, provide feedback, suggest improvements or has otherwise contributed to this package. Those that are happy to be named are (in chronological order):

- Nik Ruškuc

This package heavily uses commands that can accept an arbitrary number of arguments as inputs. I thank `egreg` for their template upon which my commands are based (<https://tex.stackexchange.com/a/72915>).

As this was my first time using keys, I thank David Carlisle for their very helpful example (<https://tex.stackexchange.com/a/542555>).

As it turns out, passing my keys to the `\draw` command of `tikz` is a little more tricky than one might expect. I thank Andrew Stacey for their solution (<https://tex.stackexchange.com/a/64237>).

I thank Partha D. for their ready to use out of the box macro for adding grid lines to a `tikz` drawing (<https://tex.stackexchange.com/a/467908>).

I also thank everybody on <https://tex.stackexchange.com> who has answered a questions or solved a problem. There are too many to list you all. Thank you.

# 2 Bugs and known problems

## 2.1 Bugs

If you discover a bug, please be so kind and send me a minimum working example of the bug in action and I will work on fixing it.

I would like this package to be as perfect as it can be but I will need your help with this as there simply are too many keys to test every combination or use case.

The following are a list of currently known bugs that will be addressed:

1. None at the moment

## 2.2 Incompatibilities

The following are a list of known problems or incompatibilities that are not scheduled to be resolved anytime soon:

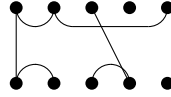
1. None at the moment

## 3 Usage

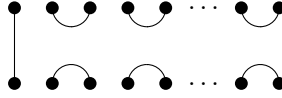
To use the package, one must understand that all diagrams are created from a basic building block called a brick.

### 3.1 Bricks

**brick** A brick is a diagram that contains no dots. For example,



is a brick whilst



`<brick>` is not a brick. The syntax for a brick contains four components and is as follows:

$$\langle \text{brick} \rangle = [\langle \text{options} \rangle] \{ \langle \text{Uedges} \rangle \} \{ \langle \text{Ledges} \rangle \} \{ \langle \text{Tedges} \rangle \}$$

`brick/<options>` where the `<options>` are described in Section 3.3.

`<Uedges>` is a list of upper non-transversal edges. An upper non-transversal edge has `Uedges/<options>` three components `<Uedges> = [<options>] {<Svertex>} {<Tvertex>}` where the `Ledges/<options>` `<options>` are described in Section 3.4.1, `{<Svertex>}` is the starting vertex `<Svertex>` and `{<Tvertex>}` is the terminating vertex of the edge. Both `{<Svertex>}` `<Tvertex>` and `{<Tvertex>}` are a  $x$ -coordinate and it is assumed that `{<Svertex>} < {<Tvertex>}`.

**list** A list of upper non-transversal edges is simply each upper non-transversal edge written after the other. For example a list with one upper non-transversal edges is

`{1}{2}`

whilst one with three upper non-transversal edges may be

`{1}{2}[level=1]{3}{4}{5}{6}`

For ease of reading this will coded as

`{1}{2}`  
`[level=1]{3}{4}`  
`{5}{6}`

`\pmdEmpty` Should a list be empty, the command `\pmdEmpty` should be used.

`<Ledges>` is a list of lower non-transversal edges. A lower non-transversal edges has the same three components as an upper non-transversal edge, namely `<Ledges> = [<options>]{<Svertex>}{<Tvertex>}`.

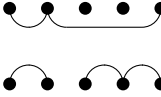
`<Tedges>` is a list of transversal edges. A transversal edges has three components `Tedges/<options> <Tedges> = [<options>]{<Tvertex>}{<Bvertex>}` where the `<options>` are described in Section 3.4.2, `{<Tvertex>}` is the top vertex and `{<Bvertex>}` is the bottom vertex of the edge. Both `{<Tvertex>}` and `{<Bvertex>}` are a  $x$ -coordinate.

An example `<brick>` and the resultant diagram is:

```

\pmdBrick[ % Options
  degree=5
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
  {4}{5}
}{ % Transversal edges
  \pmdEmpty
}

```



### 3.2 Draw commands

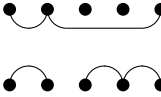
This package has three draw commands.

`\pmdBrick` draws a brick and has the syntax `\pmdBrick<brick>`.

```

\pmdBrick[ % Options
  degree=5
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
  {4}{5}
}{ % Transversal edges
  \pmdEmpty
}

```



`\pmdDiagram` draws arbitrarily many bricks separated by dots and has the syntax

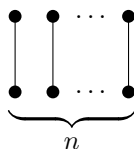
`\pmdDiagram[<options>]{<bricks>}`

where the `<options>` are described in Section 3.6 and `<bricks>` is a list of `<brick>`-s, with each brick enclosed in curly brackets.

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}

```



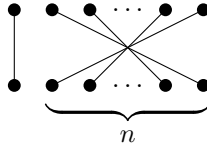
It should be noted that `\pmdBrick` is simply a wrapper for a single brick that calls `\pmdDiagram` with no diagram options. This means that, for example, the `grid` key is not available for `\pmdBrick` and `\pmdDiagram` must be used instead to access the `grid` key.

For edges that go across multiple bricks, know that the coordinate positions of the vertices extends infinitely in both directions. If using default settings, the dots between bricks occupies one vertex position. To help with counting and identifying the correct coordinate position, the `grid` flag may also be used, see Section 3.6.1.

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=3,
      brace={
        left=2,
        right=6,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{6}
      {3}{5}
    }
  }{ % Brick 2
    [ % Options
      degree=2
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{-1}
      {2}{-2}
    }
  }
}

```



`\pmdProduct` draws two diagrams on top of each other as is the case during multiplication or concatenation and has the syntax

`\pmdProduct[<options>]{<Aedges>}{<Tbricks>}{<Bbricks>}`

`diagram/<options>` where the `<options>` are described in Section 3.6.

`<Aedges>` is a list of edges that are added during the concatenation process. An added edge has two components, namely `<Aedges> = {<Svertex>}{<Tvertex>}`, where `{<Svertex>}` is the starting vertex and `{<Tvertex>}` is the terminating vertex of the collection of added edges. Both `{<Svertex>}` and `{<Tvertex>}` are a  $x$ -coordinate and it is assumed that `{<Svertex>} < {<Tvertex>}`.

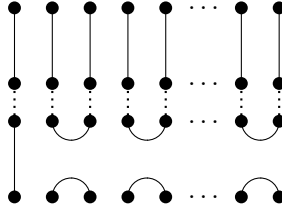
`<Tbricks>` is a list of bricks that correspond to the top diagram, with each brick enclosed in curly brackets.

`<Bbricks>` is a list of bricks that correspond to the bottom diagram, with each brick enclosed in curly brackets.

```

\pmdProduct{ % Added edges
  {1}{5}
  {7}{8}
}{ % Top diagram
  { % Brick 1
    [ % Options
      degree=5
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
      {3}{3}
      {4}{4}
      {5}{5}
    }
  }{ % Brick 2
    [ % Options
      degree=2
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }
}{ % Bottom diagram
  { % Brick 1
    [ % Options
      degree=5
    ]{ % Upper non-transversal edges
      {2}{3}
      {4}{5}
    }{ % Lower non-transversal edges
      {2}{3}
      {4}{5}
    }{ % Transversal edges
      {1}{1}
    }
  }{ % Brick 2
    [ % Options
      degree=2
    ]{ % Upper non-transversal edges
      {1}{2}
    }{ % Lower non-transversal edges
      {1}{2}
    }{ % Transversal edges
      \pmdEmpty
    }
  }
}

```



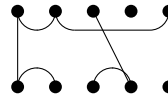
### 3.3 Brick options

The following are all of the keys that are available for bricks.

#### 3.3.1 Vertex options

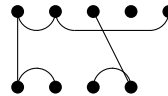
**degree** specifies the degree, that is, the number of vertices in the top and bottom row of the diagram. Must be a positive integer and must be provided unless using **degree top** and **degree bottom**.

```
\pmdBrick[ % Options
  degree=5
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}
```



**degree top** specifies the degree, that is, the number of vertices in the top (bottom) row of the diagram. Must be a positive integer and must be provided as a pair **degree top** and **degree bottom**.

```
\pmdBrick[ % Options
  degree top=5,
  degree bottom=4
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}
```



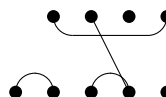
**blank top** specifies the number of blank vertices to the left of the top (bottom) row of the diagram. Default is zero.



```

\pmdBrick[ % Options
    blank top=1,
    degree top=4,
    degree bottom=5
]{ % Upper non-transversal edges
    {2}{5}
}{ % Lower non-transversal edges
    {1}{2}
    {3}{4}
}{ % Transversal edges
    {3}{4}
}

```



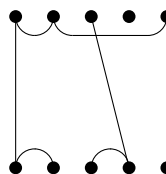
It should also be noted that the `blank top` and `blank bottom` can also be used to create more space between bricks and the dots between bricks by setting a large number. Likewise if set to `-1` and the dots is redefined to not draw, the space between bricks can be removed altogether. See Examples 13-15.

`row sep` specifies the vertical separation between rows of vertices. Default is two.

```

\pmdBrick[ % Options
    degree=5,
    row sep=4
]{ % Upper non-transversal edges
    {1}{2}
    {2}{5}
}{ % Lower non-transversal edges
    {1}{2}
    {3}{4}
}{ % Transversal edges
    {1}{1}
    {3}{4}
}

```

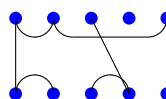


`vertices` passes through options to the `\draw` command of vertices. The default is no argument.

```

\pmdBrick[ % Options
    degree=5,
    vertices=blue
]{ % Upper non-transversal edges
    {1}{2}
    {2}{5}
}{ % Lower non-transversal edges
    {1}{2}
    {3}{4}
}{ % Transversal edges
    {1}{1}
    {3}{4}
}

```



`vertices options` allows for the redefinition of the command that draws the vertices. It has two arguments, the  $x$  and  $y$ -position of the vertex. The default is

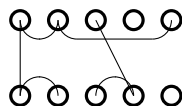
```
\fill[apply style/.expand once=\pmdraw@drawVertexOptions] (#1,#2) circle (.17);
```

An example use is

```

\pmdBrick[ % Options
  degree=5,
  vertices options={
    \draw[very thick] (#1,#2) circle (.25);
  }
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```

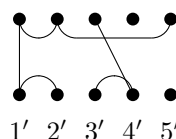


`labels` flags that allow for the drawing of labels for the vertices. Use `labels` for labels on both the top and bottom or set individually. The default is no labels.

```

labels bottom
\pmdBrick[ % Options
  degree=5,
  labels bottom
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```

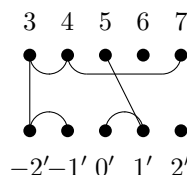


`labels start` sets the starting value of the labels for the vertices. The default is one.

```

labels top start
labels bottom start
\pmdBrick[ % Options
  degree=5,
  labels,
  labels top start=3,
  labels bottom start=-2
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```



`labels top draw` passes through options to the `\draw` and `node` command of the labels of vertices. The default is no argument.

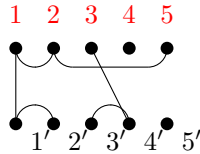
`labels bottom draw`

`labels bottom node`

```

\pmdBrick[ % Options
  degree=5,
  labels,
  labels top node=red,
  labels bottom node={right=2pt}
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```



labels top options allows for the redefinition of the command that draws the labels of the vertices.  
labels bottom options They have three arguments, the  $x$  and  $y$ -position of the vertex and the label value.  
The default for the top is

```

\draw[apply style/.expand once=\pmdraw@drawLabelTDrawOptions] (#1,#2)
  node[above=6pt,apply style/.expand once=\pmdraw@drawLabelTNodeOptions] {\(#3\)};

```

and for the bottom

```

\draw[apply style/.expand once=\pmdraw@drawLabelBDrawOptions] (#1,#2)
  node[below=6pt,apply style/.expand once=\pmdraw@drawLabelBNodeOptions] {\(#3'\)};

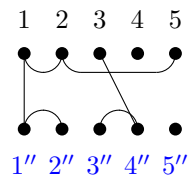
```

An example use is

```

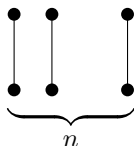
\pmdBrick[ % Options
  degree=5,
  labels,
  labels bottom options={
    \draw (#1,#2) node[below=6pt,blue] {\(#3''\)};
  }
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```



`no dots` The `no dots` flag removes the drawing of dots to the left of the current brick in diagrams. Default is to draw dots except for the first brick.

```
\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1,
      no dots
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}
```

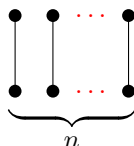


`dots draw` passes through options to the `\draw` and `node` command of the dots. The `dots node` default is no argument.

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1,
      dots node=red
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}

```



### 3.3.2 Edge options

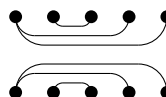
These options should be read in conjunction with Section 3.4.

`levels` specifies how many horizontal levels there are for non-transversal edges. Default is one.

```

\pmdBrick[ % Options
  degree=5,
  levels=3
]{ % Upper non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Lower non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Transversal edges
  \pmdEmpty
}

```

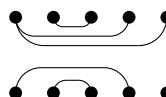


`levels top` specifies how many horizontal levels there are for upper (lower) non-transversal edges. Default is one.

```

\pmdBrick[ % Options
  degree=5,
  levels top=3,
  levels bottom=2
]{ % Upper non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Lower non-transversal edges
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Transversal edges
  \pmdEmpty
}

```

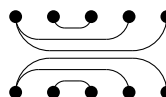


`levels sep` specifies the vertical separation between horizontal levels for non-transversal edges. Default is evenly spaced within the space available for the given number of levels.

```

\pmdBrick[ % Options
  degree=5,
  levels=3,
  levels sep=0.3
]{ % Upper non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Lower non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Transversal edges
  \pmdEmpty
}

```

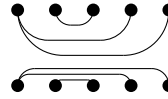


`levels sep top` specifies the vertical separation between horizontal levels for upper (lower) non-transversal edges. Default is evenly spaced within the space available for the given number of levels.

```

\pmdBrick[ % Options
  degree=5,
  levels=3,
  levels sep top=0.4,
  levels sep bottom=0.15
]{ % Upper non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Lower non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Transversal edges
  \pmdEmpty
}

```

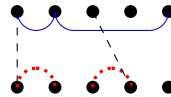


edges pass through options to the `\draw` command of their respective edge types.  
edges non-transversal The default is no argument.

```

edges upper      \pmdBrick[ % Options
edges lower      degree=5,
edges transversal edges upper=blue,
                  edges lower={red, dotted, very thick},
                  edges transversal=dashed
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```

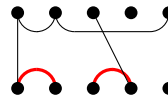


edges first flag ensures edges are drawn before vertices. The default is vertices are drawn first.

```

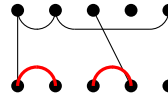
\pmdBrick[ % Options
  degree=5,
  edges lower={red, very thick},
  edges first
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```



`transversals first` flag ensures transversal edges are drawn before non-transversal edges. The default is non-transversal edges are drawn first.

```
\pmdBrick[ % Options
  degree=5,
  edges lower={red, very thick},
  transversals first
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}
```

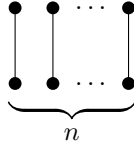


### 3.3.3 Brace

`brace` specifies instructions for the drawing of a brace with the brace keys. These are described in Section 3.5. The default is no brace is drawn.

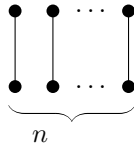
```
\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}
```





`brace draw` passes through options to the `\draw` and `node` command of the brace. Must `brace node` be given before the `brace` key. The default is no argument.

```
\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace draw=thin,
      brace node={pos=0.25},
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}
```



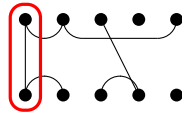
### 3.3.4 Decorations

`decorate before` provides a hook to draw additional `tikz` elements before and after the brick is `decorate after` drawn. The default is empty.

```

\pmdBrick[ % Options
  degree=5,
  decorate after={
    \draw[
      very thick,
      red,
      rounded corners=5pt
    ] (0.6, -0.4) rectangle (1.4, 2.4);
  }
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  {1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

```

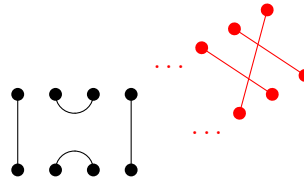


These hooks can also be used for more sophisticated manipulation of diagrams by inserting not just `tikz` elements but arbitrary code before and after draw a brick.

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=4
    ]{ % Upper non-transversal edges
      {2}{3}
    }{ % Lower non-transversal edges
      {2}{3}
    }{ % Transversal edges
      {1}{1}
      {4}{4}
    }
  }{ % Brick 2
    [ % Options
      degree=3,
      decorate before={\begin{scope}[red,shift={(1,1)},rotate=30]},
      decorate after={\end{scope}}
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{2}
      {2}{3}
      {3}{1}
    }
  }
}

```



### 3.3.5 Drawing order

For clarity, this is the default drawing order for a brick:

1. `decorate before`
2. Top row of vertices
3. Bottom row of vertices
4. Upper non-transversal edges
5. Lower non-transversal edges
6. Transversal edges
7. `decorate after`

This order can be altered using the `edges first` and `transversals first` flags.

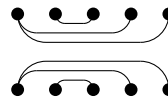
For the drawing order of a diagram and product diagram, see the `decorate before` and `decorate after` keys in Section 3.6.1.

## 3.4 Edge options

### 3.4.1 non-transversal edge options

`level` specifies the horizontal level of a non-transversal edges. Default is one.

```
\pmdBrick[ % Options
  degree=5,
  levels=3
]{ % Upper non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Lower non-transversal edges
  [level=3]{1}{5}
  [level=2]{1}{4}
  [level=1]{2}{3}
}{ % Transversal edges
  \pmdEmpty
}
```

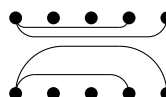


`height` specifies a manually set horizontal height of a non-transversal edges. Default is to use levels.

```

\pmdBrick[ % Options
  degree=5
]{ % Upper non-transversal edges
  {1}{5}
  [height=1.75]{1}{4}
}{ % Lower non-transversal edges
  [height=1.25]{1}{5}
  {1}{4}
}{ % Transversal edges
  \pmdEmpty
}

```



`options` allows for the redefinition of the command that draws the non-transversal edge. It has two arguments, the start and end  $x$ -position of the edge. The default for an upper non-transversal is

```

\draw[apply style/.expand once=\pmdraw@drawUedgesDrawOptions]
  (#1,\pmdraw@rowSep) arc (180:270:\pmdraw{edgeHeight}); % Draw left arch
\draw[apply style/.expand once=\pmdraw@drawUedgesDrawOptions]
  (#1+\pmdraw{edgeHeight},\pmdraw@rowSep-\pmdraw{edgeHeight})
  -- (#2-\pmdraw{edgeHeight},\pmdraw@rowSep-\pmdraw{edgeHeight}); % Draw straight line
\draw[apply style/.expand once=\pmdraw@drawUedgesDrawOptions]
  (#2-\pmdraw{edgeHeight},\pmdraw@rowSep-\pmdraw{edgeHeight})
  arc (270:360:\pmdraw{edgeHeight}); % Draw right arc

```

and for a lower non-transversal

```

\draw[apply style/.expand once=\pmdraw@drawLedgesDrawOptions]
  (#1,0) arc (180:90:\pmdraw{edgeHeight}); % Draw left arch
\draw[apply style/.expand once=\pmdraw@drawLedgesDrawOptions]
  (#1+\pmdraw{edgeHeight},\pmdraw{edgeHeight})
  -- (#2-\pmdraw{edgeHeight},\pmdraw{edgeHeight}); % Draw straight line
\draw[apply style/.expand once=\pmdraw@drawLedgesDrawOptions]
  (#2-\pmdraw{edgeHeight},\pmdraw{edgeHeight})
  arc (90:0:\pmdraw{edgeHeight}); % Draw right arc

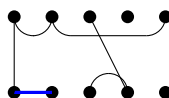
```

An example use is

```

\pmdBrick[ % Options
  degree=5
]{ % Upper non-transversal edges
  {1}{2}
  {2}{5}
}{ % Lower non-transversal edges
  [options={
    \draw[blue, very thick] (#1,0) -- (#2,0);
  }]{1}{2}
  {3}{4}
}{ % Transversal edges
  {1}{1}
  {3}{4}
}

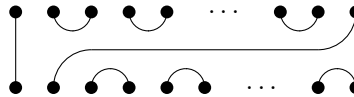
```



### 3.4.2 Transversal edge options

`height` draws transversal edges with a horizontal component and specifies the manually set horizontal height of the transversal edges. Default is to use non-horizontal transversal edges.

```
\pmdDiagram{
  { % Brick 1
    [ % Options
      degree top=5,
      degree bottom=6
    ]{ % Upper non-transversal edges
      {2}{3}
      {4}{5}
    }{ % Lower non-transversal edges
      {3}{4}
      {5}{6}
    }{ % Transversal edges
      [height=1]{10}{2}
      {1}{1}
    }
  }{ % Brick 2
    [ % Options
      degree top=3,
      blank bottom=1,
      degree bottom=2
    ]{ % Upper non-transversal edges
      {1}{2}
    }{ % Lower non-transversal edges
      {2}{3}
    }{ % Transversal edges
      \pmdEmpty
    }
  }
}
```



`options` allows for the redefinition of the command that draws the transversal edge. It has two arguments, the  $x$ -position of the edge in the top row of vertices and the  $x$ -position of the edge in the bottom row of vertices. The default is

```
\ifnum\pmdraw@ifTedgeHorizontal=0 % If drawing a straight line edge
  \draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
    (#1,\pmdraw@rowSep) -- (#2,0); % Draw straight line
\else % If transversal edge is drawn horizontally
  \ifnum#1>#2 % If edge goes from top right to bottom left
    \draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
      (#2,0) arc (180:90:\pmdraw{Tlevel}); % Draw bottom arch
    \draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
      (#2+\pmdraw{Tlevel},\pmdraw{Tlevel})
      -- (#1-\pmdraw@rowSep+\pmdraw{Tlevel}, \pmdraw{Tlevel}); % Draw straight line
    \draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
```

```

        (#1-\pmdraw@rowSep+\pmdraw{Tlevel},\pmdraw{Tlevel})
        arc (270:360:{\pmdraw@rowSep-\pmdraw{Tlevel}}); % Draw top arc
\else % If edge goes from top left to bottom right
\draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
        (#2,0) arc (0:90:\pmdraw{Tlevel}); % Draw bottom arch
\draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
        (#2-\pmdraw{Tlevel},\pmdraw{Tlevel})
        -- (#1+\pmdraw@rowSep-\pmdraw{Tlevel}, \pmdraw{Tlevel}); % Draw straight line
\draw[apply style/.expand once=\pmdraw@drawTedgesDrawOptions]
        (#1+\pmdraw@rowSep-\pmdraw{Tlevel},\pmdraw{Tlevel})
        arc (270:180:{\pmdraw@rowSep-\pmdraw{Tlevel}}); % Draw top arc
\fi%
\renewcommand{\pmdraw@ifTedgeHorizontal}{0} % Reset flag to default
\fi%

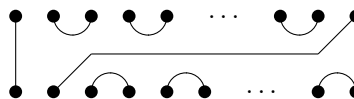
```

An example use is

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree top=5,
      degree bottom=6
    ]{ % Upper non-transversal edges
      {2}{3}
      {4}{5}
    }{ % Lower non-transversal edges
      {3}{4}
      {5}{6}
    }{ % Transversal edges
      [options={
        \draw (#2,0) -- (#2+1,1); % Draw bottom line
        \draw (#2+1,1) -- (#1-1, 1); % Draw straight line
        \draw (#1-1,1) -- (#1,2); % Draw top line
      }]{10}{2}
      {1}{1}
    }
  }{ % Brick 2
    [ % Options
      degree top=3,
      blank bottom=1,
      degree bottom=2
    ]{ % Upper non-transversal edges
      {1}{2}
    }{ % Lower non-transversal edges
      {2}{3}
    }{ % Transversal edges
      \pmdEmpty
    }
  }
}

```

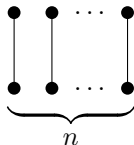


### 3.5 Brace

**brick/brace** As part of a diagram, it may be useful to draw a brace. The options of a brace are as follows:

- left** specifies the  $x$ -position of the start/left and end/right of the brace. Both must be provided.
- right**
- label** specifies the label to be printed with the brace. Default is empty.

```
\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}
```

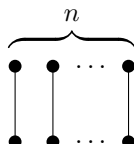


**above** The **above** flag draws the brace above the diagram. Default is below.

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n},
        above
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}

```



`options` allows for the redefinition of the command that draws the brace. It has three arguments, the  $x$ -position start and end of the brace, as well as the label of the brace. The default is

```

\ifnum\pmdraw@ifProdDiag=1 % If drawing a product diagram
                          % or if placing brace above diagram
\draw[
  very thick,
  decorate,
  decoration={calligraphic brace,amplitude=6pt},
  apply style/.expand once=\pmdraw@drawBraceDrawOptions
] (#1-0.17,\pmdraw@rowSep+0.5) -- (#2+0.17,\pmdraw@rowSep+0.5)
node[
  pos=0.5,
  above=6pt,
  apply style/.expand once=\pmdraw@drawBraceNodeOptions
] {\(#3\)}; % Draw brace on top of diagram
\else % If not drawing a product diagram or if placing brace below diagram

```



```

\draw[
  very thick,
  decorate,
  decoration={calligraphic brace,mirror,amplitude=6pt},
  apply style/.expand once=\pmdraw@drawBraceDrawOptions
] (#1-0.17,-0.5) -- (#2+0.17,-0.5)
node[
  pos=0.5,
  below=6pt,
  apply style/.expand once=\pmdraw@drawBraceNodeOptions
] {\(#3\)}; % Draw brace on bottom of diagram
\fi%

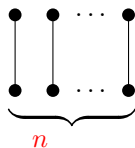
```

it should be noted that the flag `\pmdraw@ifProdDiag` is both used for when drawing a product diagram but also when placing the brace above the diagram as this clearly must be the default for the top diagram in a product diagram. An example use is

```

\pmdDiagram{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=4,
        label={n},
        options={
          \draw[
            red,
            very thick,
            decorate,
            decoration={calligraphic brace,mirror,amplitude=6pt}
          ] (#1-0.17,-0.5) -- (#2+0.17,-0.5)
          node[pos=0.25,below=6pt]{\(#3\)};
        }
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
    }
  }
}

```



## 3.6 Diagram options

### 3.6.1 For all (product) diagrams

The following options can be used for both diagrams (`\pmdDiagram`) and product diagrams (`\pmdProduct`).

- `row sep` same as `row sep` option in bricks but applied to all bricks within (product) diagram.
- `dots options` allows for the redefinition of the command that draws dots between bricks. It has two arguments, the  $x$  and  $y$ -position of the dots. The default is

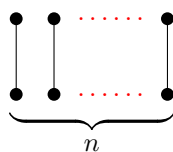
```
\draw[apply style/.expand once=\pmdraw@drawDotsDrawOptions]
  (#1,#2) node[apply style/.expand once=\pmdraw@drawDotsNodeOptions] {\(\dots\)};
```

An example use is

```

\pmdDiagram[ % Options
  dots options={
    \draw[red] (#1,#2) node {\(\dots\dots\)};
  }
]{
  { % Brick 1
    [ % Options
      degree=2,
      brace={
        left=1,
        right=5,
        label={n}
      }
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {1}{1}
      {2}{2}
    }
  }{ % Brick 2
    [ % Options
      degree=1,
      blank top=1,
      blank bottom=1
    ]{ % Upper non-transversal edges
      \pmdEmpty
    }{ % Lower non-transversal edges
      \pmdEmpty
    }{ % Transversal edges
      {2}{2}
    }
  }
}
}

```



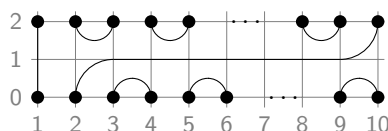
**grid** As it can get confusing where things are drawn and the different coordinate scopes between all the bricks and diagrams, the **grid** flag draws the base coordinate grid that the first drawn brick is based on. This should help with all coordinate related inquiries. Default is no grid.

It should be noted that the **grid** key is not available for `\pmdBrick` and `\pmdDiagram` must be used instead when needing a grid for a single brick only.

```

\pmdDiagram[ % Options
  grid
]{
  { % Brick 1
    [ % Options
      degree top=5,
      degree bottom=6,
    ]{ % Upper non-transversal edges
      {2}{3}
      {4}{5}
    }{ % Lower non-transversal edges
      {3}{4}
      {5}{6}
    }{ % Transversal edges
      [height=1]{10}{2}
      {1}{1}
    }
  }
  }{ % Brick 2
    [ % Options
      degree top=3,
      blank bottom=1,
      degree bottom=
    ]{ % Upper non-transversal edges
      {1}{2}
    }{ % Lower non-transversal edges
      {2}{3}
    }{ % Transversal edges
      \pmdEmpty
    }
  }
}

```



`decorate before` same as `decorate before` and `decorate after` in bricks but these are drawn  
`decorate after` before (after) all bricks are drawn. For clarity, this is default drawing order for a  
 diagram:

1. `diagram/decorate before`
2. Brick loop:
  - (a) `brick/decorate before`
  - (b) Draws brick
  - (c) `brick/decorate after`
3. `diagram/decorate after`

And this is default drawing order for a product diagram:

1. `diagram/decorate before`
2. Draws added edges

3. Top diagram:
  - (a) Brick loop:
    - i. `brick/decorate before`
    - ii. Draws brick
    - iii. `brick/decorate after`

4. Bottom diagram:
  - (a) Brick loop:
    - i. `brick/decorate before`
    - ii. Draws brick
    - iii. `brick/decorate after`

5. `diagram/decorate after`

For the drawing order of a brick see Section [3.3.5](#).

### 3.6.2 For product diagrams only

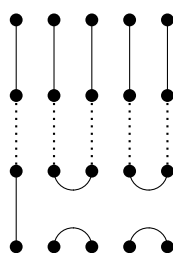
The following options can only be used for product diagrams (`\pmdProduct`).

`diagram sep` specifies the vertical separation between the bottom row of vertices in top diagram and the top row of vertices in bottom diagram. Default is one.

```

\pmdProduct[ % Options
    diagram sep=2
]{ % Added edges
    {1}{5}
}{ % Top diagram
    { % Brick 1
        [ % Options
            degree=5
        ]{ % Upper non-transversal edges
            \pmdEmpty
        }{ % Lower non-transversal edges
            \pmdEmpty
        }{ % Transversal edges
            {1}{1}
            {2}{2}
            {3}{3}
            {4}{4}
            {5}{5}
        }
    }
}{ % Bottom diagram
    { % Brick 1
        [ % Options
            degree=5
        ]{ % Upper non-transversal edges
            {2}{3}
            {4}{5}
        }{ % Lower non-transversal edges
            {2}{3}
            {4}{5}
        }{ % Transversal edges
            {1}{1}
        }
    }
}

```

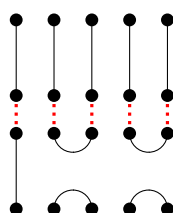


`edges added` passes through options to the `\draw` command of the added edges. The default is no argument.

```

\pmdProduct[ % Options
    edges added={red,very thick}
]{ % Added edges
    {1}{5}
}{ % Top diagram
    { % Brick 1
        [ % Options
            degree=5
        ]{ % Upper non-transversal edges
            \pmdEmpty
        }{ % Lower non-transversal edges
            \pmdEmpty
        }{ % Transversal edges
            {1}{1}
            {2}{2}
            {3}{3}
            {4}{4}
            {5}{5}
        }
    }
}{ % Bottom diagram
    { % Brick 1
        [ % Options
            degree=5
        ]{ % Upper non-transversal edges
            {2}{3}
            {4}{5}
        }{ % Lower non-transversal edges
            {2}{3}
            {4}{5}
        }{ % Transversal edges
            {1}{1}
        }
    }
}

```



## 4 Future features/work

I have attempted to make most use cases easy to use with dedicated functionality that does not require significant  $\text{\LaTeX}$  knowledge whilst at the same time provide more advanced interfaces to allow for hopefully almost complete customisability for those who put in the effort.

Having said that, please do let me know if there are features or improvements you will like to see added.

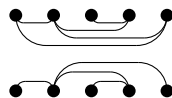
The following are some of the aims for the future for this package:

1. Fix bugs.
2. Add warning and error messages to log.
3. Allow all brick keys to work as diagram keys that apply to all bricks in a diagram. This will require setting up a flag for each key so that the diagram key sets the brick key but the brick key is not reset after drawing the first brick. This process also will need to be able to handle when a single brick has a custom special different key value and that this is reset to the digram key value and not the global default key value.
4. Allow appropriate diagram keys to work as brick keys. Notably the `grid` key.
5. Create a `tikz` key for passing options to the `tikz` environment. Have as an example a different scale for diagram.
6. The creation of user profiles that allows for fast and efficient setting of default key values that are different to the package defaults. Hence within a diagram, there can be a number of differetn diagram styles that can be accessed with one command.
7. Allow for adjusting the horizontal spacing of vertices. Need to think about making that a simple scale factor so that integer interface for edge positions is the same but then hooks will have very messy coordinates or keep it as absolute coordinates with messy edges. Alternatively, do both, allowing the user to choose which option to do and somehow distinguish between the two in the background.

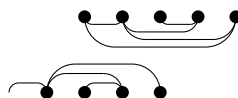
## 5 Examples

This section is simply a collection of example diagrams. The code for them can be found in the `examples` folder. Perhaps you will find them useful as a starting point for your diagrams or to see what this package is capable of.

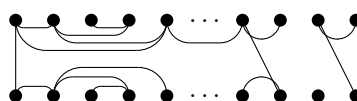
### Example 1



### Example 2

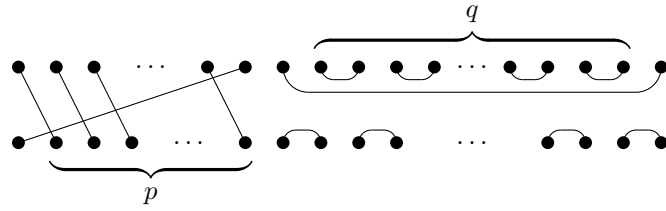


### Example 3

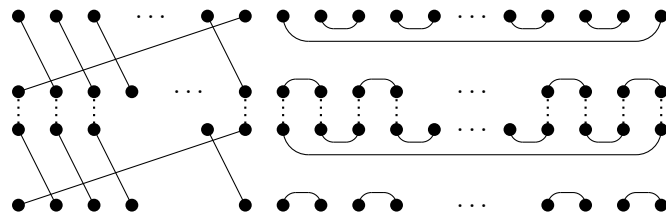




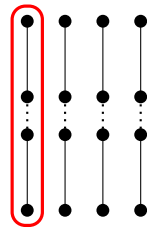
Example 4



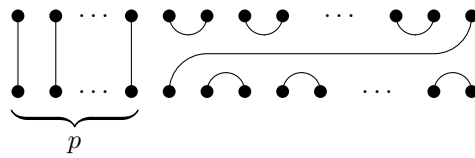
Example 5



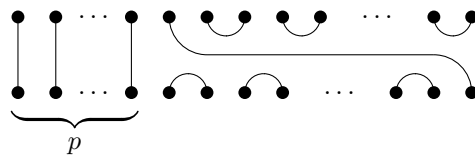
Example 6



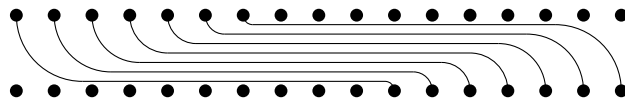
Example 7



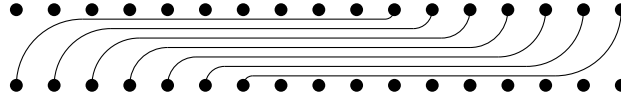
Example 8



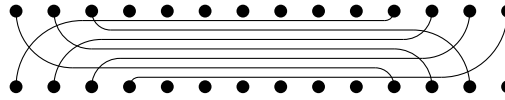
Example 9



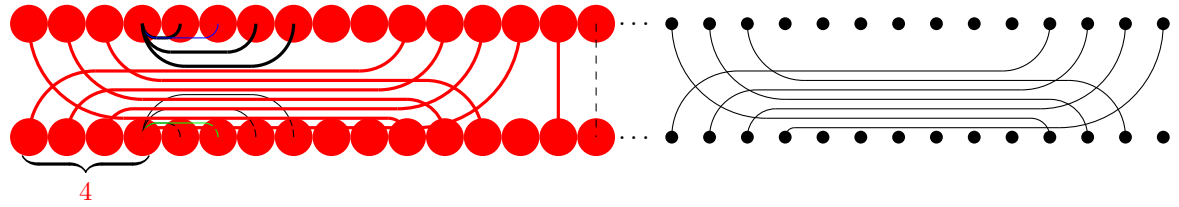
Example 10



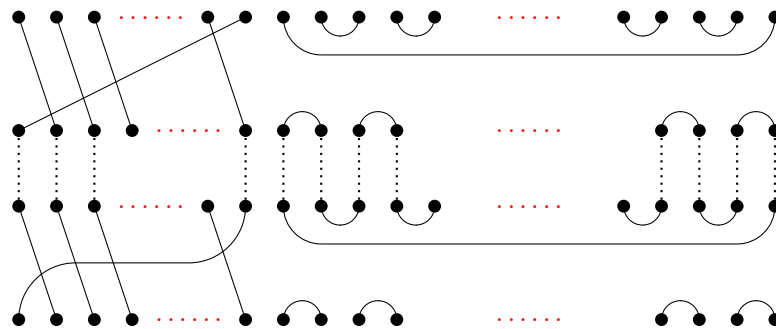
Example 11



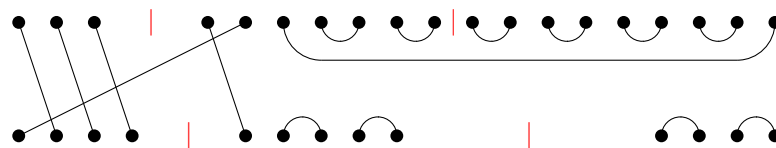
Example 12



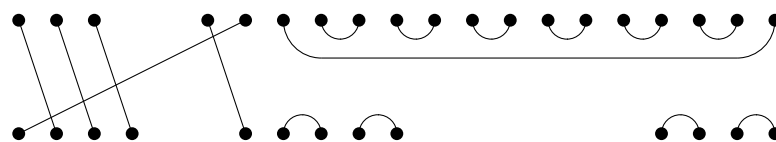
Example 13



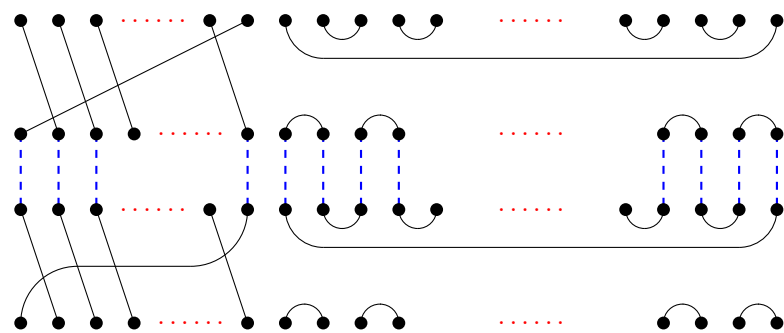
Example 14



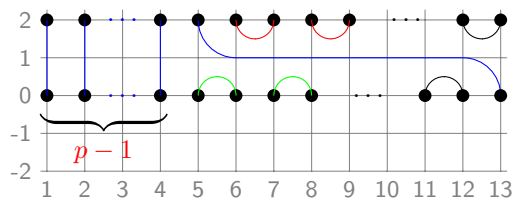
Example 15



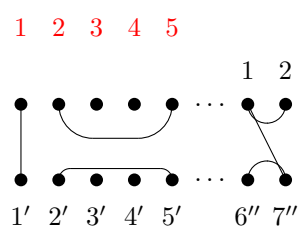
Example 16



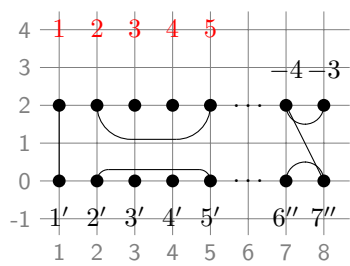
Example 17



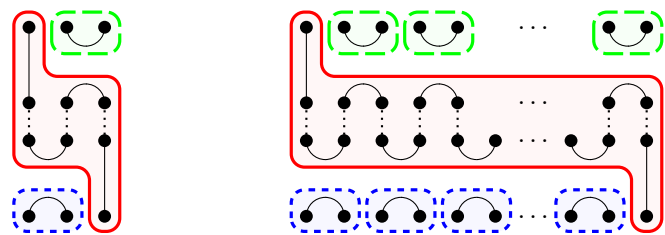
Example 18



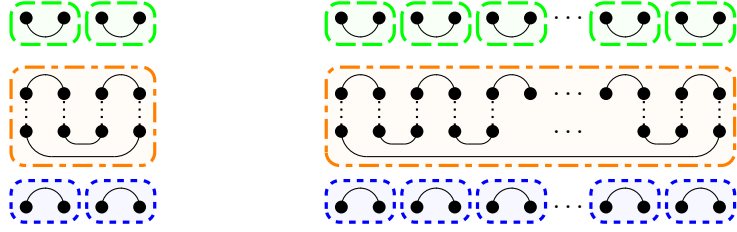
Example 19



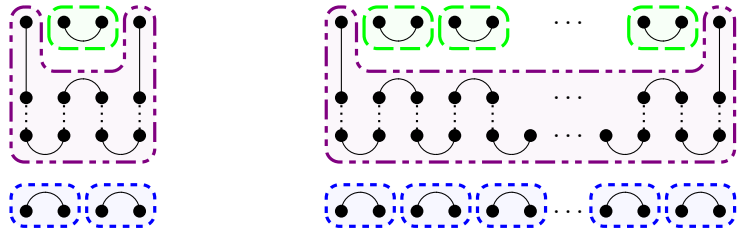
Example 20



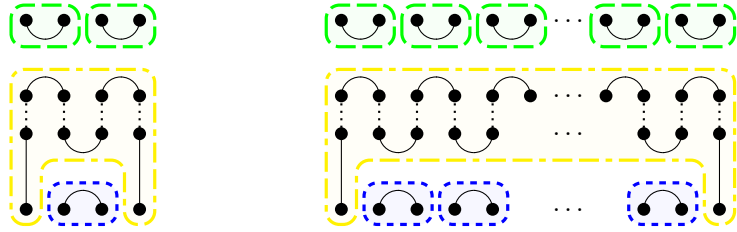
Example 21



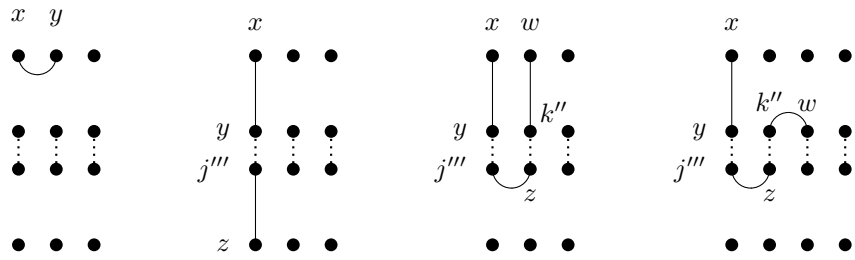
Example 22



Example 23



Example 24



Example 25

